

Math 261 - Calculus I
Los Angeles City College - Spring 2002

Dr. Kian Kaviani

Name _____

Instructions. Show your work on separate sheet(s) of papers.

1. Find the limit: (10 pts.)

$$\lim_{x \rightarrow 2} \frac{x^3 - 5x^2 + 6x}{x^3 - 8}$$

2. Find the limit: (10 pts.)

$$\lim_{x \rightarrow 2^-} \frac{1 - \frac{4}{x^2}}{1 - \frac{2}{x}}$$

3. Find $\lim_{x \rightarrow 3^-} f(x)$ where, $f(x) = \begin{cases} \frac{|x-2|}{x-2}, & x < 2 \\ x, & x > 2 \end{cases}$ (10 pts.)

4. Find the limit: (12 pts.)

$$\lim_{x \rightarrow 0} \frac{3x^2 - \sin 4x}{4x}$$

5. Find the limit: (8 pts.)

$$\lim_{x \rightarrow 0} \frac{\sin 2x}{\tan x}$$

6. Find a value for the constant "a" such that the following function will be continuous at $x = 0$ (15 pts.)

$$f(x) = \begin{cases} \frac{\sin 3x}{2x}, & x < 0 \\ a & x \geq 0 \end{cases}$$

7. Find the limit: (10 pts.)

$$\lim_{x \rightarrow 1} \left(2 - \frac{5}{(x-1)^2} \right)$$

8. For the following piecewise-defined function: (25 pts.)

$$f(x) = \begin{cases} 1 - x^2 & x \leq 0 \\ 2x + 1 & 0 < x < 2 \\ 1 - 2x^3 & x > 2 \end{cases}$$

- a. $\lim_{x \rightarrow 2^-} f(x)$
- b. $\lim_{x \rightarrow 2^+} f(x)$
- c. $\lim_{x \rightarrow 2} f(x)$
- d. $\lim_{x \rightarrow -\infty} f(x)$
- e. $\lim_{x \rightarrow 0^-} f(x)$
- f. $\lim_{x \rightarrow 0} f(x)$
- g. Is $f(x)$ a continuous function? Discuss.

h. $f(2)$

i. Graph $f(x)$